Experimental Investigation of Sediment Trap Efficiency in Reservoirs

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Abstract: Reservoir sedimentation has become one of the major problems facing water resources development projects in many countries around the world. However, only a limited number of studies has been reported in this field, particularly addressing the trap efficiency of reservoirs. In addition, whatever available studies in this area also consider few parameters governing the reservoir sedimentation. As a result, the available knowledge on trap efficiency is not very well defined. Brune curve [4] has been widely used for estimating trap efficiency of reservoirs at present, but it has several limitations, as it considers only the reservoir capacity and inflow ratio for estimating trap efficiency. The objective of this study is to formulate an improved methodology in estimating reservoir sedimentation through laboratory experiments. A small-scaled laboratory model was set-up in representing a reservoir and a series of tests were conducted by varying inflow rate, inflow sediment concentration, reservoir capacity and outflow rate. The experimental results were compared with the available theories and found that they are not very much in agreement with many of the existing theories which are mostly based on limited number of parameters. A comprehensive data analysis was performed using dimensional analysis to develop an improved relationship to estimate reservoir sedimentation incorporating many parameters governing the problem. However, the applicability of the proposed method is still limited only to the reservoirs with continuous spilling condition. In addition, only one type of sediment gradation (d_{50}) was used in the experimental runs and thus, the effect of sediment sizes is not well represented in this method. However, the relationship developed in this study could be further improved by conducting more experimental runs by varying few other parameters which are not considered in the present study.

Keywords: Reservoir sedimentation, Trap efficiency, Release efficiency, Sediment inflow rate

1. Introduction

Reservoir sedimentation is a severe problem in managing water resources development projects in many countries around the world, as it reduces the original capacity significantly which affects the irrigation, hydropower and drinking water supply, flood control and recreational activities. Rantambe reservoir in Sri Lanka is one of the reservoirs which is severely affected by sedimentation. Due to lack of reservoir management practices such as periodical sediment flushing, reservoir sediment routing and improving catchment protection to reduce soil erosion, the sedimentation of reservoirs has now becoming a major threat to many countries around the world. Though reservoir sedimentation is becoming a major threat to engineers who are responsible in managing water resources projects at present, a limited number of studies has been reported in the field of reservoir sedimentation. Brune [4] and Churchill [5] have proposed empirical methods to evaluate trap efficiency of reservoirs however, the applicability of these methods is highly limited

as their formulations consider only few parameters which affect the reservoir sedimentation. This paper presents an experimental study carried out in formulating an improved methodology to estimate reservoir sedimentation.

2. Literature Review

Very few studies have been reported in literature on reservoir sedimentation and most of which are based on analytical methods. In general, the amount of sediment accumulated in a reservoir is expressed as a percentage of

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inflow sediment quantity which is called as sediment *Trap Efficiency* (*TE*).

$$TE = \frac{\text{Amount of sediment deposits}}{\text{Amount of sediment in inflow}} \dots\dots (1)$$

Brune [4] has developed a curve relating *TE* to capacity (*V*) to annual average inflow (*I*) ratio as presented in the Figure 1, extracted from Reservoir Sedimentation Handbook by Morris et.al [7]. Brune's curve has been widely used to estimate the sedimentation of reservoirs.

Figure 1 - Brune curve [4]

This curve can also be presented in the following;

$$TE = 100 \times 0.97^{0.19 \log\left(\frac{V}{I}\right)} \dots\dots\dots (2)$$

where, *TE* = trap efficiency; *V* = reservoir capacity; and *I* = annual average inflow;

Brune [4] had considered only two parameters in his formulation namely; the reservoir capacity and average annual inflow rate and many other parameters that affect the reservoir sedimentation are not represented in his method. In addition, Brune [4] had used only normally ponded reservoirs in deriving this empirical relationship. However, his method found to be not accurate enough in estimating sedimentation quantity in reservoirs with highly variable inflows, as the sediment trapped in the reservoir is very much influenced by the sediment inflow rate.

Further, Siyam [9] has shown that Brune's [4] curve is a special case of a more general trap efficiency function given by the following equation;

$$TE = 100 e^{\beta\left(\frac{V}{I}\right)} \dots\dots\dots (3)$$

where, β is a sedimentation parameter that reflects the reduction in the reservoir storage capacity due to sedimentation.

Siyam [9] has also demonstrated that the above equation with values of $\beta = 0.0055, 0.0079$ and 0.015 would well-define the upper, median and lower Brune's [4] curves respectively as shown in Figure 1.

Churchill [5] developed a graphical relationship between Release Efficiency (*RE*) and Sedimentation Index (*SI*) as shown in Figure 2 which is extracted from Reservoir Sedimentation Handbook by Morris et. al [7].

Figure 2 - Churchill curve [5]

Sedimentation index can be defined as follows;

$$S.I = \frac{\text{Detention time}}{\text{Mean velocity}} \dots\dots\dots (4)$$

$$S.I = \frac{(\text{Reservoir capacity})^2 \times g}{(\text{Reservoir inflow})^2 \times \text{Reservoir length}} \dots\dots (5)$$

Churchill has also considered only a limited number of parameters such as detention time and mean velocity, omitting other parameters affecting reservoir sedimentation. But Trimble et.al [12] concluded that the Churchill [5] method appears to produce more realistic estimate of sediment yields than from the Brune's method [4], for reservoirs receiving sediments from an upstream reservoir. Borland [2] has also concluded that the Churchill [5] curve is somewhat superior to Brune's curve [4], in estimating reservoir sedimentation.

Verstraeten et.al [6] have stated that although the use of the Churchill curves [5] may give a better prediction of *TE* compared to Brune curves [4], but it is very difficult to obtain the necessary input data for calculating the sedimentation index for Churchill [5] curve. This is probably the reason why Brune's (1953) approach is used so extensively as opposed to Churchill [5].

Brown [3] also has also presented a correlation for TE incorporating the Capacity (V) to Watershed (W) ratio as illustrated in Figure 3.

Figure 3 - Brown's curve [3]

The relationship can also be expressed as;

$$TE = 100 \left(1 - \frac{1}{0.0021 \frac{D \times V}{W}} \right) \dots \dots \dots (6)$$

where, V = reservoir storage capacity expressed in m^3 ; and W = catchment area expressed in km^2 . D is a coefficient whose values ranging from 0.046 to 1, with a mean value of 0.1.

Here, Brown [3] also considered about the capacity (V) and watershed area (W) of the reservoir where more significant number of parameters affecting the reservoir sedimentation.

Harbor et al [8] has carried out experimental investigations on reservoir sedimentation and derived a curve which is similar to the Brune curve [4]. This relationship is given in Eq. (7).

$$TE = -22 + \left[\frac{119.6 \frac{V}{I}}{0.012 + \left(1.02 \frac{V}{I} \right)} \right] \dots \dots \dots (7)$$

Toniolo et al [11] has also carried out several experiments on reservoir sedimentation, but their results appear to be very preliminary stage and have failed to produce any conclusive results.

Bashar et al [1] have carried out bathymetric survey on Roseires reservoir which is located in Sudan, taking the baseline as the design storage capacity of the reservoir at the different levels in 1966 and compared with both Brune [4] and Churchill [5]. There he concluded that both Brune [4] and Churchill [5] methods overestimate the trap efficiency. Lewis et al [10]

has also stated about the overestimation of both Brune [4] and Churchill [5] curves.

3. Methodology

3.1 Experimental Set-up

The experimental set-up consists of an overhead tank which has dimensions of $1.2 \text{ m} \times 1.2 \text{ m} \times 1 \text{ m}$, to feed sediment laden water into the reservoir, a sediment agitator to keep sediments in suspension mode inside the overhead tank and a separate tank of 0.5 m high, 1 m wide and 2 m long, to represent a reservoir. The sediment agitator consists of an electric motor, vertical shaft with horizontal wings and a stand to fix the motor. Figure 4 shows a schematic diagram of the experimental set-up.

Figure 4 - Schematic Diagram of Experimental Set-up

The rectangular tank was modified by placing four timber plates at four corners of the tank in order to avoid water stagnation at those corners. The reservoir bed was made linearly sloping towards the dam using compacted soil to represent the model much closer to a real reservoir. The dam was made out of timber which can be moved back and forth to change the reservoir capacity (V). Actual photograph of the experimental set-up is presented in Figure 5.

The following important features were available in the experimental set-up;

- Possibility of controlling the inflow rate of sediment laden water to the reservoir by using a gate value,
- Ability to change the reservoir capacity by adjusting the downstream boundary (dam) of the model reservoir.
- Possibility of changing the spillway length by fixing different sizes of spillway

moulds on the dam. In this way, outflow from the reservoir could be changed.

- Possibility of changing inflow sediment concentration by adding different quantities of sediments to the overhead tank and mixing it with the agitator fixed to this tank.

Figure 5 - Experimental Set-up

A reddish sandy soil which passed through 1 mm sieve was used as sediments for the proposed tests. Figure 6 illustrates the particle size distribution of the sediments mixed with the inflow to the reservoir. The mean diameter (d_{50}) of the soil was found to be 0.02 mm.

Figure 6 - Particle Size Distribution of the Sediments

3.2 Experimental Procedure

Adjust the gate valve connected to the outflow pipe of the overhead tank to release known flow rate to the reservoir and allowed to spill over the pre-set length of spillway. The experiment was carried out for a duration of one hour. During the experiments, six sediment samples were taken from the inflow at different times to get the averaged sediment concentration. After the experiments are over, the sediments deposited on the reservoir bed were collected and quantified. This procedure was repeated for three different reservoir capacities 97.1 l, 119.5 l and 144.0 l, while varying the inflow sediment concentration from

0.10 kg/m³ to 1.20kg/m³. In addition, inflow rates were also changed in the range of 200 ml/s to 400 ml/s and two spillway lengths of 200 mm and 300 mm were used which controls the outflow rate from the reservoir.

4. Results and Discussion

4.1 Experimental Results

As a typical result, one set of experimental data collected from the experiments carried out for the reservoir capacity 97.1 l is given in Table 1. The results tabulated here indicates the inflow sediment concentration (C), water inflow rate to the reservoir (Q), spillway lengths (S) and dry weight of deposited sediment on the reservoir bed (W_s). Similar set of results were collected for the reservoir capacities of 119.5 l and 144.0 l.

Table 1 - Experimental Results for Reservoir Capacity 97.1 l

C/(kg/m ³)	Q/(ml/s)	S/(mm)	W_s /(g)
0.14	200.90	200	54.76
0.18	263.07	200	96.66
0.10	405.17	200	65.80
0.37	216.69	300	190.67
0.13	292.88	300	109.14
0.11	389.50	300	113.83
0.77	201.52	200	122.12
0.34	296.50	200	259.00
0.39	422.85	200	419.27
0.26	214.65	300	101.83
0.35	302.86	300	168.74
0.32	401.85	300	297.46
0.47	204.71	200	239.52
0.53	302.85	200	245.27
0.27	408.54	200	139.96
0.46	208.42	300	226.27
0.75	307.92	300	508.54
0.79	399.07	300	691.18

The variation between trapped sediment weight (W_s) and inflow rate (Q) is shown in Figure 7. It is not possible to interpret this graph as there are few other parameters influencing the sedimentation quantity (W_s).

Figure 7 - Variation between Q and W_s

The variation of trapped sediment weight (W_s) with the inflow sediment concentration (C) is illustrated in Figure 8.

Figure 8 - Variation between C against W_s

It could be seen that there is a slightly better correlation between these two parameters, though the data points are somewhat scattered that could be due to experimental errors. This figure suggests that the inflow sediment concentration (C) is one of the most influencing parameters on the amount of sediment trapped in the reservoir.

4.2 Comparison Experimental Results with Brune and Churchill Curves

Figure 9 illustrates the comparison of experimental data with the Brune curve [4]. This graph clearly shows that the experimental data are not very much in agreement with the Brune's curve [4]. Trap Efficiencies (TE) estimated from the experimental results are mostly located below the Brune's curve [4], indicating that TE 's are somewhat underestimated when compare to Brune curve.

Though the experimental data are very much scattered, it can be seen that there is an increasing trend of TE with V/I ratio, as similar to the Brune curve [4]. It could also be noted that there can be more than one value of TE for a given V/I ratio, indicating that there can be other parameters affecting TE .

Figure 9 - Comparison of experimental results with the Brune curve [4]

Figure 10 shows the comparison of experimental results with the Churchill curve [5]. In this case also, the data points are scattered within a narrow region but, gives a fare agreement with this curve than that with the Brune curve. But it can be observed that more than 50% of the results are below the Churchill curve.

Figure 10 - Comparison of the experimental results with Churchill curve [5]

It is important to highlight here that few other researchers have also reported about the overestimation of TE by the Brune [4] and Churchill [5] methods based on their studies (Bashar et al [1] and Lewis et al [10]).

As neither Brune's [4] nor Churchill's [5] methods has given a reasonable relationship for the experimental data obtained in this study, a fresh data analysis has been adopted using Dimensional Analysis.

4.3 Dimensional Analysis

The dry weight of sediment deposited (W_s) in reservoir is affected by the following parameters,

$$W_s = f\{\mu, d_{50}, Q, S, L, t, V, g, \varepsilon, \rho, \rho_s, C\} \dots (8)$$

where,

μ = Dynamic viscosity of water [ML⁻¹T⁻¹]
 d_{50} = Mean diameter of sediment particles [L]
 Q = Inflow to the reservoir [L³T⁻¹]
 S = Weir length (Spillway length) [L]
 C = Sediment concentration [ML⁻³]
 t = Time [T]
 V = Reservoir volume [L³]
 g = Gravitational acceleration [LT⁻²]
 ε = Bed roughness [L]
 L = Reservoir length [L]
 ρ = Density of water [ML⁻³]
 ρ_s = Density of sediments [ML⁻³]

The capacity of the model reservoir (V) used for the present study is dependent only on the reservoir length (L). Therefore, the parameter L is removed from the above list keeping the volume term. ε is removed as the reservoir bed in the experimental setup has been a smooth surface. The term ρ_s is also replaced by adding a term γ^* which is given by, $\gamma^* = (\rho_s - \rho)g$.

Then,

$$W_s = f\{\mu, d_{50}, Q, S, t, V, \gamma^*, \rho, \rho_s, C\} \dots (9)$$

Hence, the non-dimensional terms could be formulated as given below;

$$\frac{\rho g W_s}{\mu^2} = f\left\{ \frac{\rho^{2/3} g^{1/3} d_{50}}{\mu^{2/3}}, \frac{\rho^{2/3} g^{1/3} S}{\mu^{2/3}}, \frac{\rho^2 g V}{\mu^2}, \frac{\rho^{1/3} g^{2/3} t}{\mu^{1/3}}, \frac{C}{\rho}, \frac{\gamma^*}{\rho g}, \frac{Q g^{1/3} \rho^{5/3}}{\mu^{5/3}} \right\} \dots (10)$$

As experimental duration (t) and sediment density (ρ_s) were not varied during this study, the corresponding dimensionless terms are considered to be constants, and they do not affect the amount of deposited sediments in the reservoir for the present study. Hence, the terms; $\frac{\rho^{2/3} g^{1/3} d_{50}}{\mu^{2/3}}$, $\frac{\gamma^*}{\rho g}$ and $\frac{\rho^{1/3} g^{2/3} t}{\mu^{1/3}}$ are removed from the analysis.

4.4 Improved correlations among model parameters

The non-dimensional term representing the trapped sediment weight (W_s) was plotted against the other non-dimensional terms representing other model parameters which were obtained from the dimensional analysis.

It has already been noted that the inflow sediment concentration has a dominant effect on trapped sediment amount over the other model parameters. Figure 11 shows the relationship between non-dimensional term representing inflow sediment concentration (C) and the trapped sediment weight (W_s).

Figure 11 - Variation of non-dimensional terms representing W_s and C

Further combining the terms, inflow sediment concentration (C) and water inflow (Q) gives the sediment inflow rate (I_s) and this term has shown a good correlation with W_s where it propose an increasing trend as illustrated in Figure 12.

Figure 12 - Variation of non-dimensional terms representing W_s and CQ

Figure 12 shows the effect of inflow sediment rate (I_s) on the trapped sediment weight (W_s) in the reservoir. Combining all the model parameters, a new relationship was derived as illustrated in Figure 13, where the amount of trapped sediments in the reservoir can be estimated using all the parameters considered in this study. This new formulae incorporates the reservoir capacity (V), sediment inflow rate (I_s), and spillway length (S) which is directly correlated to outflow from the reservoir. This relationship indicates that the trapped sediment weight (W_s) will reach a maximum value with increasing the term ($I_s \cdot V/S^{1/3}$).

Figure 13 - Variation of trapped sediment weight (W_s) with the model parameters

Figure 11 suggests an equation as shown in Equation 11.

$$\frac{\rho g W_s}{\mu^2} = 3 \times 10^{-5} \left(\frac{\rho^{22/9} g^{11/9}}{\mu^{31/9}} \times \frac{I_s V}{S^{1/3}} \right)^{0.9813} \dots\dots (11)$$

Equation 11 shows the relationship between the non-dimensional terms representing trapped sediment weight (W_s) and the combined non-dimensional term of the model parameters. Sediment inflow rate (I_s) and reservoir capacity (V) presents a direct proportionality to trapped sediment weight (W_s), where spillway length (S) is inversely proportional.

5. Conclusions and Recommendations

An experimental investigation was conducted for investigating the sedimentation of reservoirs and particularly, on trap efficiency of reservoirs. Based on the series of test results, an improved correlation was derived among the parameters governing the reservoir sedimentation. Equation 11 presents a relationship between the non - dimensional terms representing trapped sediment weight (W_s) and the other model parameters such as sediment inflow rate (I_s), reservoir capacity (V) and spillway length (S).

It can also be found that the inflow sediment rate (I_s) is the most governing parameter for the sedimentation of the reservoir according to the present study.

Equation 11 can be used to estimate the amount of sediments deposited in a reservoir using other parameters with a reasonable accuracy. However, the applicability of the proposed method is still limited only to the reservoirs with continuous spilling condition. In addition, only one type of sediment gradation (d_{50}) was

used in the experimental runs and thus, the effect of sediment sizes is not well represented in this method. However, the relationship developed during this study could be further improved by conducting more experimental runs by varying few other parameters which are not considered in the present study.

As the present study concentrates only on the continuous spilling condition of reservoirs, several experiments should also be conducted with non-spilling condition. Further studies would also be needed to account the operating rules of reservoirs where sediment outflow from the reservoir will be partly restricted. Effect of reservoir shape and its orientation which are also important factors affecting the amount of sediment trapped in the reservoir, needs to be investigated.

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